

## Phase-field simulation for the growth of Boride (Fe<sub>2</sub>B) phase from Austenite phase

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**Summary** The present paper describes briefly the development of phase-field simulation for the growth of boride (Fe<sub>2</sub>B) phase from the austenite phase. In the present work, the problem in defining the free energy of a line compound such as Fe<sub>2</sub>B is approached by the assumption that it has a parabolic relationship with the boron concentration. An equilibrium condition can be obtained by one set of free energy applied in the present work. On the other hand, evaluation on the effect of temperature on the growth of boride phase using the present model shows that a higher growth of boride phase was found as the temperature increases from 1193K up to 1273K.

### BORONIZING PROCESS

Boronizing is a type of thermo-chemical treatment where boron atom is diffused into the metal substrate during high temperature process to form hard boride structure such as FeB and Fe<sub>2</sub>B. Normally it is preferable to have single layer of Fe<sub>2</sub>B on the substrate rather than having these two boride phases. The presence of single or mixed layer of boride coating mainly depends on the condition of boronizing process. In most cases FeB phase is considered to form firstly before Fe<sub>2</sub>B phase especially for the low temperature process. However, for the case of high temperature process, such as at 950-1100°C and with the longer boronizing time, single Fe<sub>2</sub>B boride phase is possible to exist.

Beside having higher hardness compared to other types of thermo-chemical treatment products, boronizing product is also believed to offer a better strength to friction wear and abrasion. Furthermore, its application in industry has been well accepted for long time such as EKabor boronizing agents have proved to be very effective in industrial practice for more than 3 decades. However less study on this process can be found in the literature compared to other types of thermo-chemical treatment. Therefore the present study made an effort to study the growth of single boride phase, Fe<sub>2</sub>B, by phase-field method of computer simulation work.

### PHASE-FIELD MODEL OF THE GROWTH OF Fe<sub>2</sub>B

Phase-field simulation offers a very good explanation on the evolution of one state to other such as in the case of phase transformation. Each state in phase-field model is governed by a number of field variable ( $\Phi$ ). For the present simulation work, Fe<sub>2</sub>B phase is set at  $\Phi=1$  and austenite phase at  $\Phi=0$ . The evolution of field variable from 0 to 1 represents the evolution of phase from austenite to Fe<sub>2</sub>B or on the other word the growth of Fe<sub>2</sub>B phase. In order to perform this simulation work, phase-field model of the boride growth is derived from Ginzburg-Landau free energy functional following the Allen-Cahn equation. This model governs the change of phase-field with time or on the other word the evolution of field variable from austenite to Fe<sub>2</sub>B. The model is as follow,

$$\frac{\partial \phi}{\partial t} = M_{\phi} \left\{ \varepsilon^2 \nabla^2 \phi + 4W\phi(1-\phi) \left( -\frac{15}{2W} \phi(1-\phi) \Delta g^{Fe_2B, Fe_s} + \phi - \frac{1}{2} \right) \right\} \dots \dots \dots (1)$$

where  $M_{\phi}$  is the kinetic parameter related to the mobility of the austenite-boride interface  $M$ .  $W$  is the potential height and  $\varepsilon_o$  is the mean value of the gradient coefficient  $\varepsilon_o$ . On the other hand,  $\Delta g$  is the chemical energy driving force, which is defined as the difference between free energy of Fe<sub>2</sub>B and austenite and the set of this energy driving force will be explained subsequently.

Beside the evolution of phase-field model, the model that governs the diffusion of boron or boron concentration profile that accompanies the growth of boride phase is also derived. This model is derived from Ginzburg-Landau free energy functional following the Cahn-Hilliard equation as follow,

$$\frac{\partial X_B}{\partial t} = \nabla \cdot \left\{ M_B(\phi, X_B, T) \left( \frac{\partial^2 g}{\partial X_B^2} \nabla X_B + \frac{\partial^2 g}{\partial X_B \partial \phi} \nabla \phi \right) \right\} \dots \dots \dots (2)$$

where  $M_B$  is diffusion coefficient of boron, and is defined as a function of diffusion coefficient of boron in austenite,  $M_B^{\gamma}$ , and boride,  $M_B^{Fe_2B}$ . Both of these variables were taken from Keddad [1].

### FREE ENERGY PROBLEM IN THE PHASE-FIELD SIMULATION OF THE GROWTH OF Fe<sub>2</sub>B

One of the big issue in developing the phase-field simulations of the growth of Fe<sub>2</sub>B is defining its free energy driving force, since it is a line compound, there is no derivative of its free energy. The common approach to solve this problem is by making an assumption that the free energy of this compound has a parabolic relationship with concentration [2,3,4]. In the present simulation works, 3 sets of free energy were chosen, where the free energy of Fe<sub>2</sub>B is fixed and the free energy of austenite is varied at 3 conditions as is shown in the fig.1.

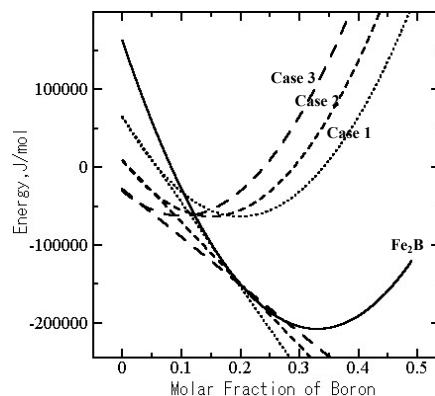


Fig.1 Free energy curve for case 1, 2 and 3 (different set of austenite free energy) and their related common tangent line

## RESULTS AND DISCUSSION

Fig. 2 (a) shows the growth of  $\text{Fe}_2\text{B}$  phase for case 1, 2 and 3. It can be seen from this figure that the growth of  $\text{Fe}_2\text{B}$  phase is higher for the case 3. However according to Fig.2 (b), case 1 is considered to give the more reliable results since the end profile of boron concentration approaching the equilibrium condition for  $\text{Fe}_2\text{B}$  phase which is around 0.33 molar fraction of boron [5].

Using the free energy of the case 1, evaluation on the effect of temperature on the growth of  $\text{Fe}_2\text{B}$  phase was made. Fig.3(a) shows the growth of  $\text{Fe}_2\text{B}$  phase at different temperatures. It can be seen from this figure that the growth of this phase is higher as the temperature increases from 1193K up to 1273K, which is also accompanied with the higher diffusion of boron (Fig.3(b)) for its related temperature. This condition indicates that an effective and efficient increasing of temperature occurs at the chosen range of temperature where a significant increasing of the kinetic of boron diffusion as well as sufficient energy is received by the system for the higher growth of  $\text{Fe}_2\text{B}$ .

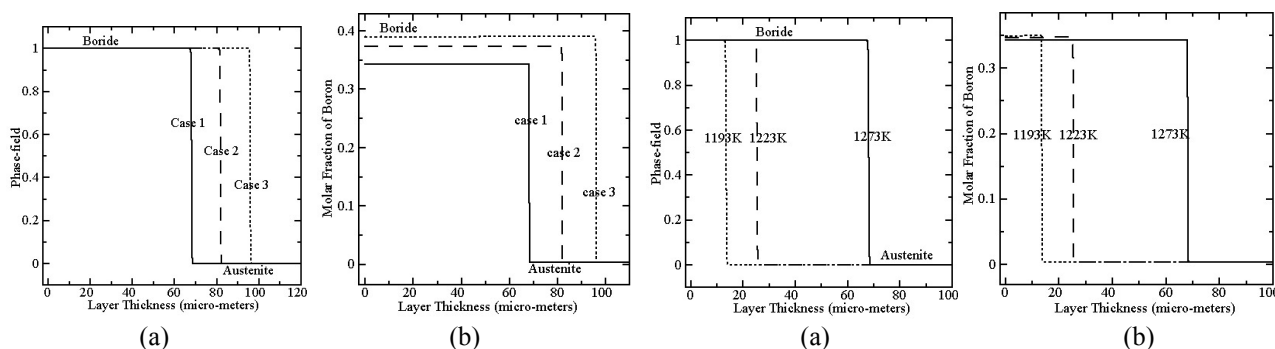


Fig.2 Boride phase growth (a) and boron concentration profile(b) for the case 1,2 and 3

Fig.3 The influences of temperature on the boride phase growth (a) and boron concentration profile (b)

## CONCLUSIONS

One-dimensional phase-field simulation of the growth of  $\text{Fe}_2\text{B}$  phase has been well performed. Three sets of free energy driving force have been determined with the assumption that both free energy of  $\text{Fe}_2\text{B}$  and austenite phase have the parabolic relationship with concentration. An equilibrium condition of  $\text{Fe}_2\text{B}$  phase can be obtained by one set of free energy and evaluation of temperature using this set of free energy indicating a higher  $\text{Fe}_2\text{B}$  phase is growth as temperature increases from 1193K up to 1273K.

## References

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